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by Eugene C. Naumann
Langley Research Center
Langley Station, Hampton, Va.

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SUMMARY

An investigation has been conducted to determine which combination of method of counting and type of load programing best retains the essential fatigue-inducing characteristics of a random time history of stress. In an earlier investigation several time histories were numerically generated and counted by various methods. The data obtained in the earlier investigation were used in this investigation to conduct axial load fatigue tests of 2024-T3 aluminum-alloy sheet specimens with notified edges. The fatigue life obtained from tests using the random peak history was used as a basis of comparison. The elimination of various sized fluctuations, due to the different counting methods, had little, if any, effect on fatigue life in tests using a random sequence of loads. Tests conducted by using ordered loading produced lives greater than the random fatigue life. The value of life in the ordered tests varied with the counting method, with statistical properties of the time history, and probably with the assumptions made in reducing the data to block form.

INTRODUCTION

The aircraft designer is well aware of the structural fatigue problems present in current aircraft. In order to offset the lack of adequate analytical design methods, common practice now is to evaluate new designs by conducting full-scale evaluation fatigue tests on prototype vehicles. If the random-load time histories encountered in service could be duplicated in a laboratory, the estimate of fatigue life from such a test would undoubtedly be considered reliable. However, existing fatigue-testing equipment is generally limited to applying simple cyclic loads. Thus, the designer must estimate service life from full-scale tests which use simplified test techniques.

Several counting methods have been devised to reduce a random-load history to numerical form. These counting methods produce several different sets of load statistics that can be used to program fatigue tests which simulate, with varying degrees of complexity, a random-load history. The purpose of this investigation is to determine whether fatigue tests, based on the load statistics obtained from the various counting methods, adequately retain the significant fatigue-inducing characteristics of a random-load history.

Four generated time histories were used in this investigation. Three of the time histories were taken from reference 1, and the fourth one, which had a bimodal power spectrum, was added to increase the scope of power spectra represented. The load statistics obtained from the various combinations of load history, counting method, and method of load-frequency-distribution simulation were used to conduct axial-load fatigue tests on 2024-T3 aluminum-alloy edge-notched sheet specimens with a theoretical elastic-stress concentration factor of four. Fatigue-life comparisons were made for each peak history.

The units used for the physical quantities defined in this paper are given both in the U.S. Customary Units and in the International System of Units (SI). Factors relating the two systems are given in reference 2.

TEST PROCEDURES

Test procedures include all the necessary preparation prior to conducting the fatigue tests. These preparations include the following: (1) preparation of the specimen; (2) a device for testing the specimen; (3) load statistics; and (4) load programs.

Specimens

The edge-notched specimen configuration (fig. 1) used in this investigation had a theoretical elastic-stress concentration factor of four. Material

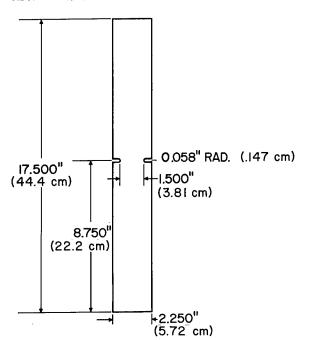


Figure 1.- Specimen configuration.

for specimens was part of a stock of commercial 0.090-inch (2.28 mm) thick 2024-T3 aluminum alloy retained at the Langley Research Center for fatigue tests. Selected tensile properties for this material are given in table I. (See ref. 3.)

A specimen-numbering system, which identifies the specimen as to material, sheet number, and location within the sheet, has been established. For example, specimen A93N2-7 is 2024-T3 material A and was taken from N2 position of sheet 93. The 7 indicates the position within the material blank (A93N2) from which the specimen blank was taken. (See ref. 4.)

Specimen dimensions are shown in figure 1. The rolled surfaces were not modified and the longitudinal surfaces were machined and notched in both edges. The notches were formed by drilling

holes to form the notch radii. Residual machining stresses were minimized by first drilling with a small drill and then gradually increasing drill sizes (increment in diameter = 0.003 inch (0.076 mm)) until the proper radius was obtained. Specimens were drilled in stacks of 10. For consistency, drills were not used more than four times before being resharpened or replaced. The notches were completed by slotting with a 3/32-inch (2.4 mm) milling tool.

Burrs left in the machining process were removed by holding the specimen lightly against a rotating cone of 00 grade steel wool. All specimens were inspected and only those free of surface blemishes in and near the notch were tested.

Machines

Three servohydraulic machines were used in this investigation. A typical block diagram of one of the machines is shown in figure 2. The loading frame had a nominal capacity of ±20,000 pounds (±89.0 KN) in axial load. Cycle rates, which depended on the load range, reached 7 cps (7 Hz). The important features of this programed load-fatigue machine are: (1) 55 discrete load levels, each identified by its own code, can be preset to any value between zero and full scale; and (2) any type of load history defined by as many as 55 discrete load levels can be programed in any arbitrary sequence by using punched cards.

A detailed description of the machine is presented in reference 5. Basically, the machine is a closed-loop servo-controlled hydraulic machine which incorporates a rather sophisticated electrical network for load selecting and checking.

Loads are monitored by either a galvanometer recorder or a null-indicating a-c bridge. The recorder is used to scan for extraneous loads, whereas the

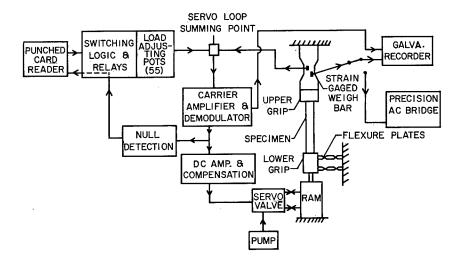


Figure 2.- Block diagram of programed axial-load fatigue machine.

a-c bridge is used to measure static loads and to check system damping. The whole system is calibrated periodically and the static-load indication is repeatable to 0.1 percent of full scale. Error in true load is less than 0.2 percent of full scale.

Load Statistics

In reference 1, a method is described for digitally generating a random time history independent of time. This time history was passed through numerical filters which had arbitrary shapes; thus, the resulting time histories had specified power spectral characteristics. Each of the power spectra had a common value for the area under the curve. (The standard deviation for each power spectrum was 1.)

Four time histories were used in this investigation: (1) white noise (time history A); (2) atmospheric turbulence (time history B); (3) single degree of freedom (time history C); and (4) a bimodal power spectrum (time history D). Time histories A, B, and C were random histories generated and analyzed in reference 1, and time history D was generated by the method described in this reference. The shape of the power spectrum for each of the time histories is shown in figure 3.

The time histories were converted to peak histories by omitting the numbers which did not define a peak (either positive or negative). This conversion, which was justified on the assumption that fatigue is more nearly cycle

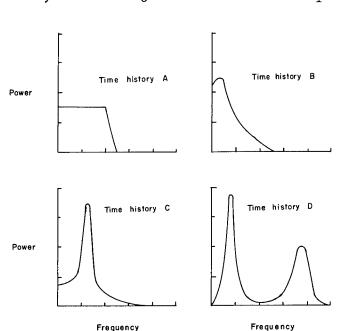


Figure 3.- Schematic representation of power spectra for four time histories. (Histories A, B, and C from ref. 1.)

dependent than time dependent, compressed the time scale so that the power spectra of the modified histories would be expected to approach the shape of the spectrum shown for time history C. (See fig. 3.) The actual shapes, however, were not investigated in this study.

The peak histories were reduced to sets of statistics which were based on several methods of counting the peak history. In addition, several methods of representing the results of the counts were used. order to facilitate counting the peak history, the generated numbers were scaled so that all numbers fell between -5.0 and 5.0 on an arbitrary scale. The smallest fluctuation counted as a cycle had a range of 0.2 on the arbitrary scale. An amplitude is defined as one-half the algebraic difference of two adjacent peaks, and a mean is defined as one-half the algebraic

sum of two adjacent peaks. A positive amplitude has a positive slope when it crosses its associated mean. In reference 1 a statistical check was made to verify that the negative and positive distributions of events were the same; therefore, only the positive distributions are considered herein.

A detailed description of each counting method used is presented in reference 6. A title and brief description of the counting methods follows:

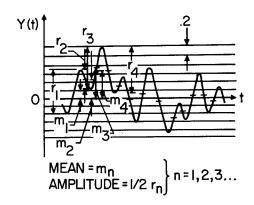
Means and amplitudes. In the means and amplitudes counting method (fig. 4(a)), each peak-to-peak fluctuation is defined by a mean and an amplitude, and, considering the entire time history, it is apparent that each mean value would have a distribution of amplitudes. (See ref. 6.) Thus, the results of this counting method can be used to develop several different distributions for test purposes. (See discussion of loading programs.)

Means and amplitudes eliminating small fluctuations.— The means and amplitudes eliminating small fluctuations counting method (fig. 4(b)) is the same as the means and amplitudes counting method except that only the peak-to-peak fluctuations which exceed 0.4 on the arbitrary scale are counted.

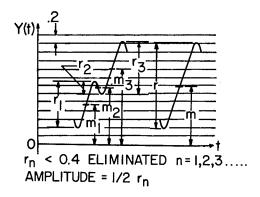
Maximum peaks between zero crossings. In the maximum peaks between zero crossings counting method (fig. 4(c)), only the amplitude of the highest peak between successive crossings of the zero reference axis is counted.

Level crossings. - The level crossings counting method (fig. 4(d)) counts the number of times the time history crosses a given level with positive slope. The number of peaks occurring in the interval between two adjacent levels, which is not necessarily the true number of peaks in the interval, is obtained by subtracting the respective number of crossings at each of these levels. (See appendix B of reference 6.)

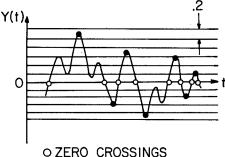
Level crossings eliminating small fluctuations. The level crossings eliminating



(a) Means and amplitudes.



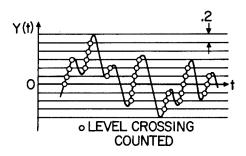
(b) Means and amplitudes eliminating small fluctuations.



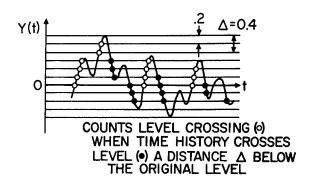
 MAXIMUM PEAK BETWEEN ZERO CROSSINGS

(c) Maximum peaks between zero crossings.

Figure 4.- Schematic representation of counting methods (from ref. 6).



(d) Level crossings.



(e) Level crossings eliminating small fluctuations.

Figure 4.- Concluded.

small fluctuations counting method (fig. 4(e)) is the same as the level crossings counting method except that the trace (with a negative slope) must cross a level a specified value lower than a given level before the higher level can be counted the next time the trace (with a positive slope) crosses. The specified value for this counting method was 0.4 on the arbitrary scale.

Load Programs

The data obtained by the various counting methods were used to program variable-amplitude fatigue tests. The following numerical relations were used to convert the distribution of peaks from the arbitrary scale (-5 to 5 in 0.2 intervals) to a load or stress scale: (1) on the arbitrary scale, O corresponded to a mean stress of $17.4 \text{ ksi } (120.1 \text{ MN/m}^2)$ on the specimen, and (2) on the arbitrary scale, 5 corresponded to the stress equal to the stress at design limit load $43.5 \text{ ksi } (300.1 \text{ MN/m}^2)$. One exception was made to assumption (2), in that for one series of tests, 4 on the arbitrary scale was made equal to the design limit

load. For these tests peak values above 4 were applied at 4.

Load programs were developed in accordance with three types of load programing: random cycle, constant-mean-block, and varied-mean-block. These load programs are as follows:

Random tests. Each of the random programs used 50 load levels, the sequence of load levels being retained from the analysis of the filtered time history. The 50 load levels corresponded to the upper limits of each of the 50 increments in the arbitrary scale. The distribution of positive peaks occurring in the positive range of the arbitrary scale for each filtered peak history and random test program is presented in table II(a). Complete descriptions of means and amplitudes for time histories A, B, and C are given in reference 1, whereas time history D is presented in table III.

Program 1: In program 1 the peaks were programed in accordance with the filtered time history. The life obtained using this load program was assumed to be the service life and was used as the basis of comparison for the lives obtained from tests using other load programs.

Program 2: In program 2 only the maximum peaks between zero crossings were applied.

Program 3: Program 3 used the peak values defined by the means and amplitudes eliminating small fluctuations counting method.

Constant-mean block tests.— The results of a given counting method were converted to the cumulative frequency distribution of stress. The distribution was divided into eight equal stress bands representing the positive peak distribution. For programs with design limit load equal to 5, each peak stress band was represented by a peak stress equal to the midstress of the band. For programs with design limit load equal to 4, the representative stresses were determined by a numerical integration process (similar to that employed in ref. 7). The number of cycles per block was arbitrarily taken to be approximately 4000 for programs with design limit load (DLL) equal to 5. For programs with DLL = 4, the number of cycles per block was selected so as to make the summation of cycle ratios approximately equal to 0.1 per block. Block sizes would then vary from 2000 to 6000.

For all block tests, each positive half cycle was followed by an equal negative half cycle. A positive half cycle is defined to be a stress excursion having a peak value algebraically larger than the mean to which it is referenced. Within each block, each load level occurred once and all cycles at that level were applied sequentially before proceeding to the next load level. Within each block, the sequence of load levels was made random in accordance with a schedule taken from a table of random numbers. A different randomization was used for each of the first 20 blocks, after which the random blocks were repeated starting with the first block.

The following load programs were developed for constant-mean block tests; the distributions used for each combination of program and peak history are given in table II(b).

Program 4: Program 4 used the cumulative frequency distribution obtained from the maximum peaks between zero crossings counting method; and had the same average distribution of positive peaks as program 2.

Program 5: The cumulative frequency distribution of positive peaks occurring in the positive range of the arbitrary scale was used in program 5. This distribution was derived from the statistics obtained in the means and amplitudes counting method. For this program, each peak was preceded and succeeded by a zero crossing.

Program 6: Program 6 used only the amplitudes from the means and amplitudes counting method. All amplitudes were applied as though they had occurred about the zero reference line of the arbitrary scale.

Program 7: Program 7 used the cumulative frequency distribution obtained from the level crossings counting method.

Program 8: Program 8 used the cumulative frequency distribution obtained from the level crossings eliminating small fluctuations counting method.

Varied-mean block tests. - The same general guide lines used for the constant-mean block tests were used for load programs in which the mean was

varied. The same eight levels were used to represent the range of stress, but instead of grouping all the means at the zero reference, three positive and three negative means were added. Therefore, seven distributions of positive peaks relative to the seven means were obtained, and each distribution was represented by 3, 5, 7, or 8 stress amplitudes. In order to facilitate programing, the means were selected at stress-band boundaries. Therefore, by using the half-band value as the representative stress, the same load levels used in the constant-mean block tests were used in these tests. With this approach there are 38 possible combinations of means and amplitudes available. As in the constant-mean block tests, each combination of mean and amplitude was programed once each block and all cycles for that combination were applied sequentially. The first 20 blocks each had a different random sequence of load levels and these random blocks were repeated starting with the first block.

The following load programs were developed for varied-mean block tests; the distributions used for each combination of peak history and counting method are given in table II(c).

Program 9: Program 9 used cumulative frequency distributions obtained from the means and amplitudes counting method.

Program 10: Program 10 used cumulative frequency distributions obtained from the means and amplitudes eliminating small fluctuations counting method.

RESULTS

The results of variable-amplitude fatigue tests of 2024-T3 aluminum-alloy specimens are presented in table IV and figure 5. In figure 5, the symbols represent the geometric mean of six tests conducted with the same load program. The scatter in the test data for a given load program seldom exceeded $1\frac{1}{3}$ to 1, a trend which is in agreement with other variable-amplitude fatigue tests conducted at the NASA Langley Research Center. (See refs. 5, 7, 8, and 9.)

For a basis of comparison the fatigue life obtained in program 1 was assumed to be service life. It would not be realistic to compare either the peak histories or the various counting methods for a given peak history by comparing the number of cycles to failure, because each peak history and counting method eliminated various numbers of the cycles from the original time history. Therefore, the basis of comparison selected was the amount (or time) of the filtered time history traversed before failure, for each combination of peak history and counting method. The basis for this conversion of cycles to time was arbitrarily selected as the number of peaks occurring in 5000 numbers in the filtered time history. It should be noted that in the original time history each generated random number was assumed to be a point equally spaced timewise from adjacent points, and that positive and negative peak distributions were symmetrical. (See ref. 1.) The equivalent life for each test condition, in increments of the time for the filtered time history, is equal to the total number of cycles to failure divided by the average total number of peaks per

Туре	Program	Attichem A Dilled
Random		● D ▼ ● History A DLL=4
	2	●
!	3	● □ ♦ □ History C
Constant-	. 4	● O □◇ ·▽ History D
mean block	5	● ○□◇
BIOCK	6	●□ ○ ◇
	7	• O\$
	8	• 🗱
Varied-	9	Ó Ø
mean	10	0 🕸
block		
		.2 .5 I 5×10 ⁶
		Life, cycles

Figure 5.- Results of variable-amplitude fatigue tests. Symbols represent geometric mean life of six tests.

5000 numbers in the filtered time history. The ability of any counting method (for a given peak history) to retain the fatigue-inducing characteristics of the peak history is evaluated by comparing the number of increments of the time history survived with the service life.

Table V presents a summary of the data obtained in this investigation. The geometric mean lives, the average number of cycles per 5000 numbers, the equivalent length of time history survived, and the normalized life for each combination of peak history and counting method used are presented in this table. The normalized lives for each peak history are shown in figure 6. Each symbol represents the geometric mean of six tests conducted with the same load program.

DISCUSSION OF RESULTS

The schematic representation of the results of the variable-amplitude fatigue tests shown in figure 5 illustrates the very small variation in mean life obtained in these tests (except shaded points) regardless of peak history or counting method used. As can be seen, more than 90 percent of the mean lives fall within the range 75,000 to 150,000 cycles.

The shaded symbols in figures 5 and 6 are data points obtained in tests with a design limit load of 4.0 on the arbitrary scale. It was found that this method produced load distributions which resulted in very short fatigue lives, and thus tended to minimize any systematic influences which might have been present. It should be noted, however, that the trends obtained in these tests

Туре	Program	●QQD∇ • History A DLL=4
Random	1	O History A DLL=5
	2	♦ History B
	3	S History D
Constant-	4	
mean block	5	ф Ф □
	6	
	7	d
	8	1 <u>4</u> 20
Varied-	9	o 🌣 🗆
mean block	10	0 0
	.:	5 1 5
		Normalized life

Figure 6.- Results of variable-amplitude fatigue tests. Symbols represent geometric mean of normalized life of six tests.

are the same with respect to the load programs as those obtained in the tests with a design limit load of 5.0 on the arbitrary scale.

A comparison of the peak values obtained from each peak history for the same counting method reveals cumulative frequency distributions which are essentially the same. Figure 7 shows the distributions: (1) the maximum peaks obtained for the means and amplitudes counting method; (2) the maximum peaks obtained for the maximum peaks between zero crossings counting method; and (3) the maximum peaks obtained for the level crossings counting method. Although statistical tests may indicate that these distributions are significantly different, their use resulted in approximately the same fatigue life.

Random Tests

The values of normalized life for each of the data points for random test programs 2 and 3 are found to be very closely grouped around a value of 1.0. (See table V and fig. 6.) The average value of normalized life for the maximum peaks between zero crossings counting method (program 2) was slightly higher than 1.0. This result seems reasonable because large amplitude cycles can be eliminated by this counting method, and fatigue life is thus increased. The average value of normalized life for the means and amplitudes eliminating small fluctuations counting method (program 3) was slightly less than 1. If these differences are real, they may be due to omitted cycles in program 2 and increased cycle amplitudes in program 3 due to the elimination of small fluctuations. Fatigue tests conducted with programs 2 or 3 would appear to provide an adequate estimate of fatigue life.

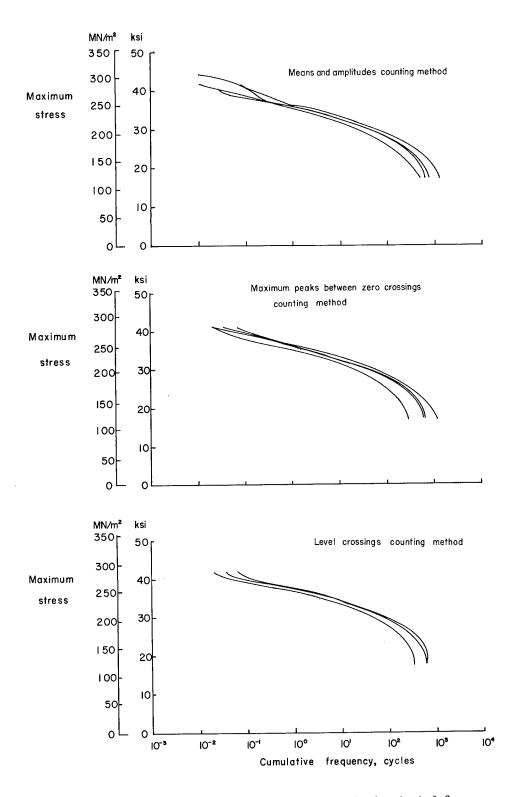


Figure 7.- Peak stress distributions of time histories tested for three counting methods.

Constant-Mean Block Tests

In the following discussion of the results of constant-mean block tests, some of the characteristics of block tests, in general, should be recalled. Among the characteristics which may influence the lives obtained in this investigation are: (1) block tests, in general, have longer lives than random tests (ref. 5); (2) the number of cycles per block (block size) may in some cases influence fatigue life (refs. 7 and 8); and (3) the assumptions made in developing the various counting methods automatically eliminate all mean stresses other than the reference mean stress, and thus reduce the strong influence of mean stress on fatigue life.

The effect on fatigue life of items (1) and (2) is discussed in some detail in the cited references and will not be reiterated here. The importance of item (3) will be noted in particular in subsequent discussions of the data obtained in this investigation and therefore requires additional comment. In reference 1, an analysis of the probability of equaling or exceeding a given value of a mean is presented. Figure 8 (data from ref. 1) shows the probability distributions for the peak histories used in this investigation. In figure 8, the slope of the curve is a measure of the dispersion of individual means about the reference mean. Therefore, when a given counting method compressed all means to the reference mean, the effect on fatigue life will be greatest for the peak history with the greatest dispersion of mean stresses.

The average value of the normalized life for constant-mean block tests using load programs 4, 5, 7, and 8 are greater than 1.0. (See table V and

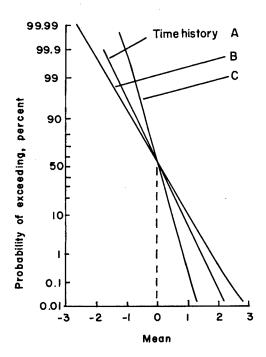


Figure 8.- Representation of mean stress dispersion for three time histories.

fig. 6.) Each group of data for a given counting method would be expected to be ordered according to increasing mean stress dispersion of the peak histories. This trend is present to some degree but is not completely established.

The results of tests using load program 6 show a very decided increase in life over the reference life (program 1). The primary reason for this increase appears to be the suppression of mean stress dispersion, which reduced the peak stress values for each peak history and thus produced a net increase in fatigue life. These results agree qualitatively with those reported in reference 10.

From the foregoing discussion it appears reasonable to expect that the use of constantmean block tests generally will produce normalized lives greater than 1.0. The value of normalized life will vary with the counting method, with statistical properties of the time history, and probably with the assumptions made in reducing the data to block form.

Varied-Mean Block Tests

The results of the varied-mean block tests (table V and fig. 6) show that a wide range of values of normalized life are obtained. The data do not indicate a consistent trend. However, it should be noted that the effects due to techniques associated with block tests using multiple means have not been fully investigated. The variations in the results cannot be explained. It does not appear that this type of load programing provides a consistent estimate of fatigue life.

CONCLUDING REMARKS

Fatigue tests were conducted by using the peak values from four random peak histories, each having a different power spectrum. The peak values were assigned arbitrary stress values and were applied to edge-notched sheet specimens of 2024-T3 aluminum alloy. Companion fatigue tests were conducted by using the results of several counting methods and employing three testing techniques: (1) retention of original sequence, (2) application in a block sequence with constant mean stress, and (3) application in blocks with varied mean stress. The results were compared to determine the combination of counting method and testing technique which retained the essential fatigue-inducing characteristics of a generated random time history.

The tests using random peak histories resulted in essentially equal fatigue lives for all four power spectra. Although the power spectra of the four time histories were quite different, the peak stress distributions were very similar.

The tests which used random sequences modified according to several counting procedures resulted in fatigue lives equivalent to those obtained before counting. Apparently, lives were not affected by the fact that the counting procedures systematically eliminated certain fluctuations in the time history.

The constant-mean block tests resulted in fatigue lives generally greater than those for the peak histories. Suppression of mean stress dispersion, which is inherent in block tests, is probably the most important factor/responsible for this behavior. In addition, earlier tests have shown that block tests produced longer lives than random tests if the same stress-frequency distribution is used. The degree of variation is dependent upon both counting method and statistical properties of the time history.

Varied-mean block tests produced widely dispersed lives which were not amenable to reasonable interpretation.

The results of this investigation indicate that additional experimental and analytical work is necessary to determine the basic fatigue-inducing characteristics of a given time history.

Langley Research Center,
National Aeronautics and Space Administration,
Langley Station, Hampton, Va., October 26, 1964.

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TABLE I.- TENSILE PROPERTIES OF MATERIAL TESTED

[Data from reference 5; 2024-T3 (147 tests)]

Property	Average	Minimum	Maximum
Yield stress (0.2% offset), ksi	52.05	46.88	59.28
	358.6	323.0	408.4
Ultimate tensile strength, ksi	72.14	70.27	73.44
	497.0	484.2	506.0
Total elongation (2 in. (5.08 cm) gage length), percent	21.6	15.0	25.0

TABLE II.- LOAD PROGRAMS USED FOR VARIABLE-AMPLITUDE FATIGUE TESTS OF 2024-T3 ALUMINUM-ALLOY SPECIMENS

$$S_{\text{mean}} = 17.4 \text{ ks1 (120.06 MM/m}^2)$$

(a) Random tests

	-T		·
	Д	Program 3	021 021 031 04 05 05 05 05 05 05 05 05 05 05
	Peak history	Program 2	1447481110000000000000000000000000000000
numbers	Pes	Program 1	524 524 525 524 524 525 525 525 525 525
) filtered	Ü	Program 3	0813725787888128441 201748787888128441 201748471199
ss per 5000	ak history	Program 2	7% 74% 75% 75% 75% 75% 75% 75% 75% 75% 75% 75
positive peaks	Peak	Program 1	484447648888484848488848888888888888888
of	Д	Program 3	ovuquestaguut-401
of occurrence	Peak history	Program 2	4年88887848111171111111111111111111111111
Relative frequency of	Pea	Program l	1387343889411-001 048489899
Relative	А	Program 3	012500000000000000000000000000000000000
	Peak history	Program 2	\$%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
	Per	Program 1	\$\psi \text{4.650} \psi \text{8.04} \psi \text{9.04} \psi \text{9.04} \psi \text{9.04} \psi \text{9.04} \psi \text{9.04} \psi \text{9.06} \psi
Stress	a)	MN/m ²]	1869 1978 1979 1979 1979 1979 1979 1979 197
Stress		ks1	010000000000000000000000000000000000000
	Load		0.4666664444444446600000000000000000000

^aFor tests in which design limit load was equal to 4.0 on the arbitrary scale increase each amplitude 20% not to exceed 25.6 ksi (176.5 MM/ μ ²).

TABLE II.- LOAD PROGRAMS USED FOR VARIABLE-AMPLITUDE FATIGUE TESTS OF 2024-T3 ALUMINUM-ALLOY SPECIMENS - Continued

(b) Constant-mean block tests

Load an		ess Ltude	Relati	ve frequency of	f occurrence of		ks per	
level	ksi	MN/m ²	Program 4	Program 5	Program 6	Program 7	Program 8	
	Peak history A (DLL = 4.0)							
1 2 3 4 5 6 7 8	2.40 5.40 8.40 11.50 14.70 17.80 20.95 24.00	16.6 37.3 58.0 79.4 101.4 122.8 144.6 165.6	517 579 522 367 182 66.5 15.5 2.25 2251.25	595 730 612 359 175 64.5 15.5 2.25	1705 2148 1575 678 165 26.5 1.8 .1	310 647 521 367 181 66.5 15.5 2.25 2110.25	93 562 544 367 181 66.5 15.5 2.25 1831.25	
			Peak h	istory A (DLL =	= 5.0)		,	
1 2 3 4 5 6 7 8	1.63 4.89 8.16 11.42 14.68 17.94 21.21 24.47	11.3 33.7 56.3 78.8 101.3 123.8 146.4 168.8	1081 1287 1009 483 134 19.67 1.50 •33 4015•5	934 1475 1027 439 120 18 1.2 -3 4014.5	1365 1651 803 178 18.5 .5 0 4016.0	524 1490 1280 547 -150 22.5 1.5 -4 4015.4	763 1505 1118 478 131 19.6 1.3 -3 4016.2	
]	Peak history B				
1 2 3 4 5 6 7 8	1.63 4.89 8.16 11.42 14.68 17.94 21.21 24.47	11.3 33.7 56.3 78.8 101.3 123.8 146.4 168.8	1372 1224 823 456 112 20 2.5 0 4009.5	1515 1339 715 330 83 14 1.5 0	2000 1340 520 127 12.5 .4 .1 0	800 1400 1090 530 155 23 2 0 4000.0	400 1400 1320 650 200 27.5 2.2 .2 3999.9	
				Peak history C				
1 2 3 4 5 6 7 8	1.63 4.89 8.16 11.42 14.68 17.94 21.21 24.47	11.3 33.7 56.3 78.8 101.3 123.8 146.4 168.8	1022 1477 956 401 135 11 2 0 4004.0	1171 1425 888 386 108 17 1.5 0 3996.5	1000 1400 1100 400 88 11.3 .6 .1	800 1500 1070 465 139 24 2 0	1000 1000 1260 550 163 24.3 2.5 .1	

TABLE II.- LOAD PROGRAMS USED FOR VARIABLE-AMPLITUDE FATIGUE TESTS OF 2024-T3 ALUMINUM-ALLOY SPECIMENS - Concluded

(c) Varied-mean block tests

Mean	stress	T 3	Str		Relative frequency of occurrence at positive peaks per 5000 filtered numbers			peaks			
		Load level		itude	Peak h	istory A	Peak h	Peak history B		Peak history C	
ksi	mn/m ²		ksi	MN/m ²	Program 9	Program 10	Program 9	Program 10	Program 9	Program 10	
1.09	7•52	1 2 3	1.63 4.89 8.16	33.7	2 1.4 1.2	0.2	29 8.5 2.2	10 7•5 1•5	0 0 0	0 0	
7.61	52.51	1 2 3 4 5	1.63 4.89 8.16 11.42 14.68	56.3	40 43 49 14 4	6 26 40 15 4	220 130 41 7.8 1.1	120 115 59 14.8 1.1	8 5.6 3.4 1.8	1 3 4.2 1.7	
14.14	97•57	1234567	1.63 4.89 8.16 11.42 14.68 17.94 21.21	101.3	274 325 236 114 27 4	114 308 250 119 30 5	450 300 117 29.2 3.7 .1	300 400 182 51 6.3 .2	190 260 182 73 16.3 1.4	115 260 220 82 16.2 1.3	
17.4	120.06	12345678	17.94 21.21	56.3 78.8 101.3 123.8	188 256 214 85 22 4	13.4 200 225 90 23 4 •5	600 44 168 37•5 4.2 .3 0	400 640 311 90 9 2 0	700 890 610 235 57 7.7 •3	500 1100 660 273 59 7.6 •3	
20.66	142•55	1 2 3 4 5 6 7	1.63 4.89 8.16 11.42 14.68 17.94 21.21	123.8	370 325 251 104 27•9 4•5	11.4 296 262 118 31 4.5	460 310 118 29 3	300 410 203 60 6•5 0	200 270 185 77 16 1.7	100 250 250 80 18 1.7	
27•19	187.61	1 2 3 4 5	1.63 4.89 8.16 11.42 14.68	33.7 56.3 78.8	43 46 37 16 3	15 31 32 16 3	285 72 34 8.1 .8	110 116 57 15.5	7 5 4.5 1.9	1 32 4.6 2.4 •7	
33.71	232.60	1 2 3	1.63 4.89 8.16	11.3 33.7 56.3	1.2 1.4 .4	•5 •5 •5	35 9 1.2	9 8 1	000	0	

TABLE III .- FREQUENCY OF OCCURRENCE OF MEANS AND AMPLITUDES FOR TIME HISTORY D (BIMODAL)

	Total	6556 1088673 1088673 10887 108	106426
ļ	+5.6	н	н
ŀ	-2.6	н н	α
Ì	+2.4	011 W40000404	1,4
	-2.4	4 W40W4004044	17
•	+2.2	のすろののアラララティスのユ	64
	-2.2	しいしゅうしょうちょう しょうし	35
	+2.0	るでできらぬみのりょうてくらるて121201	188
	-2.0	クトクキトクサロロロロレー 1111111 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	123
	+1.8	80000000000000000000000000000000000000	327
	-1.8	00001222222220000	361
- us	+1.6	2522247474253801v00110	656
of mean	-1.6	48 xx x z z x x x x x x x x x x x x x x x	638
	4°T+	74457750001 100004 100001	1398
occurrence	4°τ-	# \$\infty \cong \c	2466 1324 1398
g g	+1.2	2 1 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2	
Frequency	-1.2	294 1730 1730 1730 1730 1730 1730 1730 1730	2284
Freq	+1,0	2007 2007 2007 2007 2007 2007 2007 2007	3979
	-1.0	250 250 250 250 250 250 250 250 250 250	6166 3781
	8.01	15 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4	
	9.0	10000000000000000000000000000000000000	6012
	9.0+	2577788 25777788 25777788 25777788 2577778 2577778 2577778 257778	8525
	9.0-	22222 22222 222222 2222222222222222222	8290
	4.0+	たままでによる 4 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2	1.0984
	4.0-	#65 1000000000000000000000000000000000000	10815
	+0.2	25.5% 1011100 1007100 10071100 10071100 10071100 10071100 10071100 10071100 10071100	12254 12455 12444 10815 10984 8290
	-0.2	24 4 8 8 9 9 1 1 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6	12455
	0.0	28.88.80 2011120 28.88.45 2011120 201120 2011120 2011120 2011120 2011120 2011120 2011120 2011120 20111	12254
	tude		Total

TABLE IV.- RESULTS OF VARIABLE-AMPLITUDE FATIGUE TESTS OF 2024-T3 ALUMINUM-ALLOY SPECIMENS

(a) Peak history A (design limit-load = 4.0 on scale)

Program	Specimen	Cycles	Program	Specimen	Cycles
1	A33N2-2 A86N2-3 A85N2-3 A79N2-5 A87N2-10 A34N2-2	36,015 36,015 33,215 32,305 28,245 28,070	2	A85N2-2 A37N2-7 A30N2-8 A30N2-6 A85N2-5 A37N2-8	31,045 26,670 25,025 24,710 23,940 23,695
	Geometric mean	32,140		Geometric mean	25 , 760
3	A79N2-10 A83N2-3 A84N2-6 A86N2-4 A37N2-9 A30N2-2 Geometric mean	30,555 29,225 27,125 23,975 22,085 21,070	4	A78N2-1 A87N2-6 A86N2-5 A79N2-8 A28N2-2 A83N2-9	31,272 29,089 29,055 27,049 27,109 23,668
5	A87N2-1 A79N2-9 A79N2-6 A86N2-9 A30N2-7 Geometric mean	35,536 33,019 32,984 29,310 26,757 26,197 30,400	6	A85N2-7 A82N2-7 A80N2-7 A30N2-4 A34N2-10 A86N2-6 Geometric mean	119,828 119,793 101,631 101,631 88,366 88,191
7	A37N2-10 A30N2-3 A82N2-6 A34N2-5 A82N2-4 A84N2-5 Geometric mean	30,593 29,323 24,298 24,158 24,123 24,123 26,000	8	A84N2-10 A78N2-2 A28N2-8 A84N2-2 A82N2-8 A28N2-9 Geometric mean	24,220 23,585 23,375 15,925 21,124 21,124 21,350

TABLE IV.- RESULTS OF VARIABLE-AMPLITUDE FATIGUE TESTS OF 2024-T3 ALUMINUM-ALLOY SPECIMENS - Continued

(b) Peak history A (design limit-load = 5.0 on scale)

Program	Specimen	Cycles	Program	Specimen	Cycles
1	A82N2-1 A82N2-2 A84N2-4 A81N2-10 A79N2-4 A87N2-2	98,053 94,710 94,710 91,560 89,250 87,640	2	A80N2-4 A78N2-9 A78N2-10 A84N2-7 A80N2-9 A84N2-3	92,085 79,170 73,990 72,905 70,245 66,710
3	A82N2-3 A81N2-7 A78N2-6 A87N2-3 A83N2-10 A84N2-8 Geometric mean	91,945 89,600 80,325 74,585 73,920 68,775	<u>}</u> +	A87N2-5 A81N2-8 A82N2-10 A110N2-10 A87N2-8 A85N2-8 Geometric mean	99,767 91,351 88,376 83,180 81,605 76,399 86,460
5	A83N2-7 A79N2-1 A106N2-3 A85N2-4 A105N2-9 A87N2-4 Geometric mean	88,353 85,669 77,641 74,326 74,326 72,646 78,610	6	A106N2-4 A106N2-7 A98N2-8 A107N2-10 A98N2-10 A107N2-7 Geometric mean	248,654 237,959 224,931 212,822 177,439 177,369 211,300
7	A98N2-7 A106N2-10 A105N2-7 A106N2-9 A107N2-8 A98N2-9 Geometric mean	88,391 82,004 76,379 74,462 63,148 60,243	8	A106N2-2 A79N2-3 A107N2-9 A105N2-6 A105N2-8 A85N2-6 Geometric mean	84,892 76,493 66,493 64,953 62,407 62,372 69,100
9	A109N2-2 A110N2-7 A108N2-1 A108N2-2 A110N2-9 A93N2-6 Geometric mean	71,330 60,235 58,415 56,105 52,710 51,415	10	All6N2-4 Al00N2-5 Al08N2-3 All6N2-3 All6N2-5 Al01N2-4 Geometric mean	55,265 49,490 49,490 49,175 49,175 44,555

TABLE IV.- RESULTS OF VARIABLE-AMPLITUDE FATIGUE TESTS OF 2024-T3 ALUMINUM-ALLOY SPECIMENS - Continued

(c) Peak history B

Program	Specimen	Cycles	Program	Specimen	Cycles
1	A91N2-5 A113N2-10 A111N2-10 A17N2-9 A104N2-7 A102N2-7 Geometric mean	173,215 161,175 151,900 143,115 141,890 140,245	2	Al05N2-4 Al12N2-6 A90N2-9 A97N2-7 Al03N2-9 Al05N2-2 Geometric mean	92,575 92,575 78,120 77,420 77,105 75,705 81,935
3	All2N2-8 A92N2-7 Al03N2-3 Al03N2-2 A91N2-2 Al03N2-4 Geometric mean	119,280 104,440 100,765 99,540 93,975 79,520 98,850	4	A90N2-1 A117N2-6 A96N2-2 A95N2-9 A94N2-7 A109N2-8	136,570 126,070 122,220 115,500 114,135 112,700
5	A95N2-8 A91N2-4 A96N2-10 A99N2-7 A91N2-7 A97N2-10 Geometric mean	152,390 145,040 143,955 142,415 134,400 132,580 141,700	6	A88N2-7 A111N2-6 A99N2-3 A111N2-8 A111N2-9 A89N2-7 Geometric mean	502,985 474,985 422,590 413,980 366,870 354,165 419,200
7	All2N2-5 A89N2-6 Al02N2-3 A97N2-5 A96N2-4 Al02N2-1 Geometric mean	99,995 96,460 91,315 91,315 91,315 84,560 92,368	8	A100N2-10 A88N2-6 A113N2-8 A111N2-2 A97N2-2 A89N2-10 Geometric mean	72,660 71,785 71,575 65,030 62,475 56,455 66,390
9	Al22N2-1 Al07N2-2 Al34N2-2 Al22N2-3 Al34N2-4 Al07N2-3 Geometric mean	165,550 165,550 163,485 137,220 124,635 117,495	10	A122N2-7 A123N2-9 A134N2-6 A132N2-7 A134N2-9 A133N2-6 Geometric mean	137,060 133,420 123,620 117,145 112,000 103,040

TABLE IV.- RESULTS OF VARIABLE-AMPLITUDE FATIGUE TESTS OF 2024-T3 ALUMINUM-ALLOY SPECIMENS - Continued

(d) Peak history C

Program	Specimen	Cycles	Program	Specimen	Cycles
1	A91N2-3 A101N2-1 A91N2-8 A105N2-5 A96N2-9 A102N2-4 Geometric mean	100,695 95,060 93,065 92,750 90,825 75,075 90,878	2	A97N2-1 A92N2-5 A103N2-1 A92N2-8 A11N2-1 A104N2-1 Geometric mean	97,615 87,850 83,790 83,265 76,860 67,445 82,274
. 3	A114N2-1 A108N2-6 A102N2-10 A96N2-5 A95N2-7 A115N2-1 Geometric mean	94,185 82,215 81,305 76,405 65,905 65,555 76,950	24	A92N2-10 A109N2-7 A90N2-3 A100N2-1 A117N2-8 A93N2-10 Geometric mean	125,965 118,930 114,660 113,540 112,000 101,605
5	AlOlN2-2 All7N2-9 AlO9N2-7 A97N2-6 AlO5N2-1 A90N2-2 Geometric mean	125,930 115,080 113,890 103,110 101,780 96,425 108,900	6	All3N2-7 Al04N2-5 A95N2-1 A99N2-4 A88N2-9 A89N2-7 Geometric mean	144,900 139,055 136,815 132,790 126,385 114,310
7	Al02N2-2 All1N2-5 Al4N2-1 A89N2-8 A95N2-6 A96N2-3 Geometric mean	108,710 108,640 100,135 83,685 83,685 78,120	8	AlllN2-7 AlolN2-9 AloON2-9 A97N2-3 A88N2-10 A88N2-8 Geometric mean	100,450 90,230 79,450 79,450 76,615 74,200 82,870
9	A132N2-6 A133N2-2 A98N2-5 A123N2-10 A92N2-1 A93N2-1 Geometric mean	172,060 162,540 159,040 144,900 139,265 124,880 149,600	10	A123N2-6 A122N2-8 A132N2-10 A122N2-6 A123N2-7 A122N2-10 Geometric mean	139,475 124,915 115,780 107,730 106,575 100,625

TABLE IV.- RESULTS OF VARIABLE-AMPLITUDE FATIGUE TESTS OF 2024-T3 ALUMINUM-ALLOY SPECIMENS - Concluded

(e) Peak history D

Program	Specimen	Cycles
1.	Al29N2-5 A9N3-1 Al25N2-6 Al27N2-9 A7N3-10 Al31N2-4	160,370 160,370 157,460 150,290 139,475 113,050
	Geometric mean	145,800
2	A108N2-5 A128N2-2 A127N2-4 A129N2-10 A102N2-6 A128N2-7 Geometric mean	121,590 121,170 109,550 103,495 100,520 84,490
3	Al26N2-7 Al29N2-7 A3N3-7 Al30N2-4 A3N3-8 Al31N2-2 Geometric mean	132,685 130,305 125,895 124,180 123,130 105,210

TABLE V.- SUMMARY OF VARIABLE-AMPLITUDE FATIGUE-TEST DATA ANALYSIS

	Normal- 1zed life	1.00	1.06	66.	-	-	1	-	1	!	
tory D	Units Factor of time (a) (b)	88.5	¥.1	87.7	-	-	-		!	ļ	-
Peak history	Factor (a)	1647.5	1126.3	1403.1					1	2 1 1	
H	Geometric mean life, cycles	145,800 1647.5	106,000	123,100 1403.1		1 1 1 1 1		1 1 1		1	
	Normal- ized life	1.00	1.03	96.	1.42	1.27	1.42	1.16	1.12	1.65	դդ. ւ
tory C	Factor of time (a) (b)	684.0 132.9	136.3	127.6	189.2	169.0	189.2	154.2	556.7 148.9	218.7	0.161 0.509
Peak history	Factor (a)	0.489	603.5	603.0	603.5	644.5	0.489	603.0	556.7	0.489	603.0
H	Geometric mean life, cycles	90,878	82,274	76,950	114,200	108,900	129,400	93,000	82,870	149,600	115,200
	Normal- ized life	1.0	1.01	%	1.49	ਹ.।	2.77	1.12	1.07	.97	1.16
tory B	Factor of time (a) (b)	265.3	268.3	京春	395.9	320.4	734.3	296.7	283.4	258.4	309.9
Peak history	Factor (a)	570.9	305.4	389.2	305.4	7,42.2	570.9	311.3	234.3	570.9	389.2
H	Normal Geometric ized mean life life,	151,440	81,935	98,850	120,900	141,700	419,200	92,368	66,390	147,500	120,600
5.0)	Normal- ized life	1.00	1.10	1.01	1.8	-97	2.28	1.07	1.18	.63	.63
Peak history A (DLL = 5.0)	Units of time history (b)	825.6 112.1	123.2	113.6	141.1	109.0	255.9	119.8	132.4	70.3	70.7
story A	Factor (a)	825.6	612.7	699.5	612.7	721.1	825.6	613.0	522.0	825.6	699.5
Ревк р1	Units Normal Geometric film ized life, (b)	92,580	75.470	79,430	86,460	78,610	211,300	73,430	69,100	58,020	49,430
(0.4	Normal- ized life	1.00	1.08	.93	ਰ•ਾ	1.08	3.19	1.09	1.05	l	
Peak history A (DLL = 4.0)	Factor of time (a) (b)	38.9	42.0	36.3	0.74	42.2	825.6 124.2	45°4	6.04	ļ	
lstory A	Factor (a)	825.6	612.7	699.5	612.7	721.1	825.6	613.0	522.0		1
Peak hi	Program Geometric number mean life, cycles	32,140	25,760	25,410	28,800	30,400	102,500	26,000	21,350		1
Program		ч	a	ĸ	4	10	9	7	ω	6	10

Practor = average number of positive peaks occurring after counting per unit of 5000 filtered numbers.

bunits of time history = Geometric mean life Factor

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